Deep Convolutional Networks with Tunable Speed-Accuracy Trade-off for Human Activity Recognition Using Wearables

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Abstract—Activity recognition plays a critical role in various applications such as medical monitoring and rehabilitation. Deep learning has recently made great development in wearable based human activity recognition (HAR) area. However, real HAR applications should be adaptive and flexible to available computational budget. So far, this problem has rarely been explored. In contrast to existing deep HAR researches focusing on static networks, this paper aims to investigate adaptive networks, which can adjust their structure conditioned on available computing resource to trade off between accuracy and speed. We for the first time present an adaptive convolutional neural network by dynamically modifying network width. Specifically, first, instead of normal convolution, the network is stacked by lower-triangular convolutional layers in order to remove the impact of activation statistics caused by varying widths. Second, instead of fixed sampling, we perform random sampling over width, which can provide smooth control for trade-off between accuracy and speed. As a consequence, the networks with different widths are simultaneously trained as subnetworks by accumulating their losses during each iteration. On multiple HAR datasets such as UCI-HAR, PAMAP2 and OPPORTUNITY, extensive experiments verify that the proposed approach can consistently provide further improved efficiency on top of state-of-the-art CNNs for HAR. Finally, evaluations are conducted on a Raspberry Pi platform to demonstrate its usefulness and practicality.

Index Terms—Sensor, convolutional neural networks, activity recognition, deep learning, wearable device

I. INTRODUCTION

URING the past decade, there is a rapid development in Internet of Things (IoT) and sensing technology, which enables various motion sensors such as accelerometer and gyroscope embedded in smartphones or other wearable devices to record physical activities for automatic recognition task. Due to small size and low cost, sensor based human activity recognition (HAR)[1], [2], [3] has played an indispensable role in human-computer interaction and ubiquitous computing, which has gained a lot of attention in various application scenarios such as wellbeing, smart home, sports monitoring, medical monitoring and rehabilitation[4], [5]. In essence, HAR can be treated as a typical pattern recognition problem[6], [7]. Traditional recognition algorithms such as decision tree, support vector machine and naive Bayes have been devoted to the design of shallow handcrafted features[8], which heavily rely on specific domain knowledge or human experience. However, such handcrafted features such as the mean, variance, frequency and amplitude of Fourier transform are hard to infer complex human activities, which leads to a lower chance to build a successful HAR system.

Deep learning, especially convolutional neural network (CNN)[9] has recently provided an alternative to overcome above limitations. In deep learning, the feature extraction and inference model often can be performed simultaneously. The high-level features can be extracted automatically through stacking deeper layers rather than being manually designed, which makes it very suitable for inferring complex activities. Although CNN has significantly improved the accuracy of state-of-the-art HAR algorithms[10], [11], [12], the low-latency or realtime feedback may be very critical. Besides accuracy, computational complexity is another key factor to be considered. Actually, highly miniaturized wearable devices often have a very limited computational budget. Real HAR applications typically pursue best accuracy under a resource-constrained platform, where an accuracy/speed trade-off should be preferably considered.

On the other hand, in order to deploy HAR applications under realistic conditions, one has to maintain model flexibility to adapt to varying computational budgets (e.g., varying hardware platforms)[13], [14]. Thus, fast inference alone is not always sufficient. For example, as far as we know, there are over 20 brands (e.g., iPhone, Samsung and Google) of phones, which have a limited yet variable computing power. It will lead to drastically different inference times, even for the same model. For satisfactory inference speed, low-end phones have to run smaller models with lower accuracy due to limited computing power, while high-end phones can run larger models to produce higher accuracy. As a result, the inference time constraint has to be conditionally dependent for specific hardware platforms. Even for the same phone, the computing power could potentially vary due to resource consumption caused by other running apps. On the
whole, real HAR algorithms must be not only simply fast, but also flexible to varying computational budgets, which have been rarely explored in HAR area.

Our core research motivative is to design an adaptive deep network in HAR scenario, which can adapt to varying computational budgets. A common idea is to modify width (the number of active channels), instead of depth (the number of layers). Specially, the simplest strategy is to train N networks at different widths, which can dynamically perform switch between them for trade-off between accuracy and speed. However, there are obvious drawbacks for the N-Width strategy. Due to varying widths, the activation statistics in each sub-network is variable. Thus, N networks have to be separately trained. If N is small, one only can provide coarse-grained control for accuracy-speed trade-off. Instead, if N is increased to a fine-grained level, it will lead to a great increase in training burden. As a consequence, it needs to store multiple offline trained versions, which will inevitably lead to larger memory footprint. Moreover, it takes necessary communication cost (e.g., time) to download new models for switch.

In this paper, we propose an adaptive deep network in HAR scenario, which can maintain model flexibility to adapt to varying computational budgets at runtime, without the need of downloading new models for switch on wearable devices. We address above challenges from two technical aspects. First, instead of N fixed sampling, we perform random sampling over width, where the networks at arbitrary width can be simultaneously trained as subnetworks by accumulating their losses during each iteration. In other words, we only need to train a single network executable at any width, which can provide a smooth control over accuracy/speed trade-off. Second, to avoid potential performance degradation caused by varying activation statistics at any width, the network is built using lower-triangular convolutional layers rather than normal convolution. Evaluations are performed on multiple public HAR datasets, namely UCI-HAR, PAMAP2, UniMib-SHAR, OPPORTUNITY and WISDM. In contrast to static models, the proposed model can provide a smooth control over accuracy/speed trade-off, which can dynamically adapt deep HAR to available computing resource. The contributions of this paper are three-fold:

First, we for the first time propose an adaptive deep network executable at any width for HAR, which can provide a smooth control over accuracy/speed trade-off via random sampling approach.

Second, when switching at arbitrary width, we avoid potential performance degradation caused by varying activation statistics via replacing normal convolution with lower-triangular convolution.

Third, without need of downloading new models, we perform actual evaluations at test time on a Raspberry Pi platform, which verify the practicibility and usefulness of the proposed model.

The rest of this paper is structured as follows. Section II reviews the related works. Section III presents the structure of adjustable CNN in HAR scenario. Section IV details experimental setup, performance comparison and analysis, which indicates the advantage of our proposed model. Finally, conclusions are made in Section V.

II. RELATED WORKS

Recent developments in deep learning have significantly improved the accuracy of state-of-the-art HAR algorithms, which can greatly alleviate the burden of handcrafted feature designing procedures. In HAR scenario, Zeng et al.[9] at the earliest time exploited CNN to automatically extract the local dependency and scale invariant features from raw acceleration time series. Yang et al.[15] presented a novel CNN constructed by multiple iterations of convolutional and pooling layers, where convolution and pooling operation are combined for feature extraction of HAR. Hammerla et al.[16] evaluated various deep, convolutional and recurrent approaches on several benchmark datasets, which shows how they surpass traditional shallow machine algorithms for a large variety of HAR tasks. Huang et al.[17] introduced a shallow CNN that uses cross-channel communication in HAR scenario, where graph neural network is used to realize a comprehensive interaction between different channels for capturing discriminative features of raw sensor signals. In order to capture temporal dynamics for HAR, Ordóñez et al.[18] proposed a novel network architecture called DeepConvLSTM consisting of convolutional and recurrent units, which significantly outperforms CNN alone. On the whole, those above network architectures are often static. However, most wearable devices only have a limited, yet dynamic computing power due to their varying hardware platforms. Thus, HAR algorithms should be adaptive or flexible to available computational budgets. It deserves deeper research into adaptive network architectures for HAR, which so far has been rarely explored.

In another line of research, deep learning has made major breakthroughs in machine vision, in which the trade-off between speed and accuracy is at the forefront of this research. Many previous works have been devoted to designing lightweight networks. For example, Howard et al.[19] and Sandler et al.[20] presented a series of lightweight networks called MobileNet, which can adaptively scale model size for different vision tasks by adjusting width and resolution multipliers. Zhang et al.[21] and Ma et al.[22] proposed a family of small networks called ShuffleNet, which can effectively decrease computational overhead by exploiting channel shuffle and pointwise group convolution. There are also other model compression techniques known as weight or channel pruning, decomposition, and knowledge distillation[23]. Despite their success, these above methods make the trade-off decision during network design or training stage. Instead, we aim to trade off accuracy and speed at inference time. Several prior approaches have been proposed for inference time control by modifying network depth. One mainstream idea is to perform early-exits or early-stopping inference according to available computing resource[24]. In order to reduce computation, other research efforts focus on layer skipping or dropping[25], [26]. These depth-modulation
techniques are orthogonal to resource-constrained control.

Recently, the idea of width-modulation has been exploited to control the trade-off between accuracy and speed. Using pruning technique, Kim et al.[27] trained one network in terms of a specific number of sparsity ratios, which accordingly provides a fixed set of internal networks. All these networks are jointly optimized to form a final N-in-1 nested network, which enables multiple hierarchical classification tasks through a single network. Similarly, Yu et al.[28] trained one network with multiple versions of a specific number of predefined N-widths, which can be switched during inference time. As a result, they only can provide coarse-fined control due to a limited number of switchable networks, where multiple copies of the trained model need to be stored. From the viewpoint of width, Lu et al. first investigated how it affects the performance of deep networks. Moreover, they presented a universal theorem for the width-bounded ReLU networks[29]. Yu et al.[30] and Huang et al.[31] exploited two-step knowledge distilling technique to train an Universally Sizable Network. However, most width-modulation techniques have been devoted to various vision applications, which has rarely been exploited in ubiquitous HAR scenario. Actually, there have always been increasing demands to deploy HAR system on resource-constrained wearable devices. While many prior researches have focused on designing a static deep network for HAR, it is very ineffective to deploy a single neural network across different wearable devices with variable computing resource. Because a new type of device usually requires a new network architecture, one has to build and train a new model from scratch. In this paper, we focus on the first time tackle this challenge in HAR scenario by designing an adaptive network that can provide assured performance on available computing resource.

### III. MODEL

As indicated above, our research motive is to train a single network for HAR task, which can run at arbitrary width. Without loss of generality, the basic form of feature aggregation within a specific convolution layer can be formulated as[23], [32]:

$$y = \sum_{i=1}^{k} \omega_i x_i$$  \hspace{1cm} (1)

where $n$ is the number of channels (width)$x_i$, and $w_i$, $i \in \{1, 2, \cdots, k\}$ correspond to the input feature vector and learnable coefficient respectively, and $y$ is an output. The network width plays an important part in trading off accuracy and speed: the larger number of channels often provides better accuracy, but sacrifices inference speed. In principle, the performance of wider networks should be no worse than that of its slim version, which has been proved by the theory of channel-wise residual learning[31], [32], [33]:

$$0 \leq \delta_{k+1} \leq \delta_k \leq \delta_{k_0}, \delta_k = |y^n - y^k|, \delta_{k+1} = |y^n - y^{k+1}|$$  \hspace{1cm} (2)

where $y^k$ and $y^{k+1}$ is the sum of the first $k$ and $k+1$ channels respectively, i.e., $y^k = \sum_{i=1}^{k} \omega_i x_i$ and $y^{k+1} = \sum_{i=1}^{k+1} \omega_i x_i$. $k_0$ denotes the minimum width. The above inequality 2 indicates that there is an upper bound $\delta_{k_0}$ for residual errors between fully aggregated features $y^n$ and partially aggregated features $y^k$, which continuously decreases as the network width $k$ increases. As the upper bound exists, a single network could run at arbitrary width by varying $k$ from $k_0$ to $k_n$. To train a single network with any width, an intuitive idea is to accumulate losses randomly sampled from all sub-networks at arbitrary widths. In order to access all widths, fixing lower bound (e.g., smallest width 0.125x) and upper bound (e.g., largest width 1.0x), we randomly sample $n-2$ widths over the open interval (0.125, 1.0). At each training iteration, besides the lower and upper bound, the network is trained with $n-2$ randomly sampled widths by performing gradient back-propagation from accumulated losses with all widths, where ground truth is used as training label for HAR.

Actually, the random sampling method can be seen as a kind of knowledge distillation, which transfers knowledge learned from full-width network to subnetworks at smaller widths in each iteration. Specifically, we first train a large network at full width, then its learned knowledge is transferred to a small network, which is then trained with predicted soft labels. Using this rule, we can train the tunable-width network at largest width, smallest width and other randomly sampled widths all together during each training iteration. That is to say, this training idea is naturally supported by knowledge distillation: the ground truth is directly used to train the network at largest width, while the predicted label by the network at the largest width is used as the training label for the networks at other widths. The experimental results verify that the classification accuracies do not decay rapidly as the network width decreases. This training scheme can implement well without extra computational and memory overhead[23], [31].

On the other hand, if the network is switched in a multi-
width scenario, the issue of varying activation statistics at different widths has to be considered. For example, if \( k = 1 \), the Eq.1 can be explicitly written as[34]:

\[
[y] = [\omega_{11}]x_1 = [\omega_{11}x_1]
\]  

(3)

and if \( k = 2 \) and \( k = 3 \), it is:

\[
\begin{align*}
    y_1 &= \left[ \begin{array}{cc}
        \omega_{11} & \omega_{12} \\
        \omega_{21} & \omega_{22}
        \end{array} \right] \left[ \begin{array}{c}
        x_1 \\
        x_2
        \end{array} \right] = \left[ \begin{array}{c}
        \omega_{11}x_1 + \omega_{12}x_2 \\
        \omega_{21}x_1 + \omega_{22}x_2
        \end{array} \right] \\
    y_2 &= \left[ \begin{array}{ccc}
        \omega_{11} & \omega_{12} & \omega_{13} \\
        \omega_{21} & \omega_{22} & \omega_{23} \\
        \omega_{31} & \omega_{32} & \omega_{33}
        \end{array} \right] \left[ \begin{array}{c}
        x_1 \\
        x_2 \\
        x_3
        \end{array} \right] = \left[ \begin{array}{c}
        \omega_{11}x_1 + \omega_{12}x_2 + \omega_{13}x_3 \\
        \omega_{21}x_1 + \omega_{22}x_2 + \omega_{23}x_3 \\
        \omega_{31}x_1 + \omega_{32}x_2 + \omega_{33}x_3
        \end{array} \right] \\
    y_3 &= \left[ \begin{array}{c}
        \omega_{11}x_1 \\
        \omega_{11}x_1 + \omega_{12}x_2 \\
        \omega_{11}x_1 + \omega_{12}x_2 + \omega_{13}x_3
        \end{array} \right] = \left[ \begin{array}{c}
        \mu_1^{(1)} \\
        \mu_1^{(2)} \\
        \mu_1^{(3)}
        \end{array} \right]
\end{align*}
\]  

(4)

For simplicity and without loss generality, \( y_1 \) can be formulated as:

\[
y_1 = \begin{cases} 
    \omega_{11}x_1 & \text{if } k = 1 \\
    \omega_{11}x_1 + \omega_{12}x_2 & \text{if } k = 2 \\
    \omega_{11}x_1 + \omega_{12}x_2 + \omega_{13}x_3 & \text{if } k = 3 
\end{cases}
\]  

(6)

The expected value of \( y_1 \) may vary at different widths:

\[
\begin{align*}
    E[y_1^{(1)}] &= E[\omega_{11}x_1] = \mu_1^{(1)} \quad k = 1 \\
    E[y_1^{(2)}] &= E[\omega_{11}x_1 + \omega_{12}x_2] \\
    &= E[\omega_{11}x_1] + E[\omega_{12}x_2] \\
    &= \mu_1^{(1)} + \mu_2^{(2)} \quad k = 2 \\
    E[y_1^{(3)}] &= E[\omega_{11}x_1 + \omega_{12}x_2 + \omega_{13}x_3] \\
    &= E[\omega_{11}x_1] + E[\omega_{12}x_2] + E[\omega_{13}x_3] \\
    &= \mu_1^{(1)} + \mu_2^{(2)} + \mu_3^{(3)} \quad k = 3
\end{align*}
\]  

(7)

Clearly, three cases (\( k = 1, k = 2 \) and \( k = 3 \)) could not follow the same distribution. In other words, the switch between multi-width will lead to varying statistics of \( y_1 \) in batch normalization[34], which may deteriorate classification performance. In order to guarantee the same distribution in two-width or three-width case, one has to ensure that \( E[\omega_{12}x_2] = 0 \) or \( E[\omega_{12}x_2] = E[\omega_{13}x_3] = 0 \). In a similar way, the expected value of \( y_2 \) may vary at different widths:

\[
\begin{align*}
    E[y_2^{(2)}] &= E[\omega_{21}x_1 + \omega_{22}x_2] \\
    &= E[\omega_{21}x_1] + E[\omega_{22}x_2] \\
    &= \mu_2^{(2)} \quad k = 2 \\
    E[y_2^{(3)}] &= E[\omega_{21}x_1 + \omega_{22}x_2 + \omega_{23}x_3] \\
    &= E[\omega_{21}x_1] + E[\omega_{22}x_2] + E[\omega_{23}x_3] \\
    &= \mu_2^{(2)} + \mu_3^{(3)} \quad k = 3
\end{align*}
\]  

(8)

To ensure \( E[y_2^{(2)}] = E[y_2^{(3)}] = 0 \), one has to set \( E[\omega_{23}x_3] = 0 \). As a result, the weights in convolutional layers can be formulated as:

\[
\begin{bmatrix}
    \omega_{11} & 0 & 0 \\
    \omega_{11} & \omega_{22} & 0 \\
    \omega_{11} & \omega_{32} & \omega_{33}
\end{bmatrix}
\]  

(9)

Without loss generality, when above two-width or three-width case is extended to multi-width case, one feasible solution is to constrain the weight matrices in convolutional layers to be lower-triangular[32], [34], [35], which can address this problem well. The overview of the design is illustrated in Fig.1. Thus, we aim to design a convolutional network consisting of triangular layers (Fig.2), which can run at arbitrary width to perform activity recognition tasks. The pseudo code in Algorithm 1 summarizes the overall procedure of model training.

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**Algorithm 1 Convolutional Network with Tunable Speed-Accuracy Trade-off**

**Input:** A, Convolutional Network  
**Input:** \( E_{\text{degs}} \), number of training iterations  
**Input:** N, number of randomly sampled width  
**Input:** \( L_{\text{max}} \), sampled width upper bound, \( L_{\text{min}} \), sampled width lower bound  
**Input:** x, training data processed by sliding window, \( y^* \), labels processed by sliding window

1: Initialize network A  
2: for \( i = 1 \) to \( E_{\text{degs}} \) do  
3: Load x, \( y^* \)  
4: Sample N-2 widths between the interval \([L_{\text{min}}, L_{\text{max}}]\)  
5: \( S = \{L_{\text{min}}, a_1, \ldots, a_{N-2}, L_{\text{max}}\} \)  
6: Clearing gradients  
7: for \( j \) in \( S \) do  
8: Set network’s width as \( j \)  
9: \( y = A(x) \)  
10: Loss = criterion(\( y^* \), y)  
11: Loss backward  
12: end for  
13: Network optimize  
14: end for

---

Fig. 2. Channels connection of lower-triangular convolution at different widths

---

**IV. EXPERIMENT**

In this section, three types of experiments are conducted. In part one, we aim to analyze how HAR accuracy is affected as network width is varied. In order to do this, we measure the effect of triangular convolutional layer at different widths. In part two, we perform further ablation studies with regard to the statistics of batch normalization[34]. We also analyze
### TABLE I
SIMPLE DESCRIPTION OF DATASET

<table>
<thead>
<tr>
<th>Attribute</th>
<th>Dataset</th>
<th>UCI-HAR</th>
<th>WISDM</th>
<th>PAMAP2</th>
<th>UniMib-SHAR</th>
<th>OPPORTUNITY</th>
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### TABLE II
SIMPLE DESCRIPTION OF MODEL’S STRUCTURE

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### TABLE III
SIMPLE DESCRIPTION OF NEURAL NETWORK PARAMETER

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### TABLE IV
TEST ACCURACY(%)

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<th>PAMAP2</th>
<th>UniMib-SHAR</th>
<th>OPPORTUNITY</th>
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<tr>
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<tr>
<td>Other Researches</td>
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### TABLE V
MAC OF DIFFERENT DATASET

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<th>Width Multiplier</th>
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<th>WISDM</th>
<th>PAMAP2</th>
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</thead>
<tbody>
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<td>0.748M</td>
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the influence of several key factors such as the number of randomly sampled width (N), width lower bound and width sampling rule. Finally, the actual operation of adaptive width network is evaluated on a resource-constrained Raspberry Pi platform.

A. Datasets

1) UCI-HAR[45]: Wearing a Samsung Galaxy S2 smartphone on the waist, a group of 30 volunteers between 19 and 48 years old joined in the data collection process. Each volunteer was instructed to perform a set of predefined activities consisting of Standing, Lying, Sitting, Walking, Walking upstairs and Walking downstairs. At a sampling frequency of 50Hz, the triaxial acceleration and angular velocity signals are recorded by the embedded accelerometer and gyroscope in the smartphone.

2) WISDM[46]: The WISDM research team members from Fordham University created the dataset. Wearing an Android based smartphone in their trouser pants pocket, 29 subjects were supervised to perform six kinds of activities including Walking, Jogging, Ascending stairs, Descending stairs, Sitting, and Standing. The accelerometer signals are collected every 50ms, i.e., 20 samples/second.

3) PAMAP2[47]: The dataset is composed of sensor recordings collected from 9 volunteers, who were instructed to perform 18 physical activities, consisting of 12 specific activities (Walking, Cycling, Rope jumping, etc.) and a few optional activities (Watching TV, Playing soccer, Car driving, etc.). Each volunteer wore three Colibri wireless inertial measurement units (IMU), which were placed over the dominants chest, hand and ankle respectively. The sampling rate of 100Hz is down-sampled into 33.3Hz for further analysis. A heart rate monitor with sampling rate 9Hz is used to estimate sport intensity.

4) UniMib-SHAR[48]: The dataset is composed of 11771 samples collected from 30 subjects whose ages range between 18 and 60 years. Wearing a Samsung Galaxy Nexus i9250 phone with an accelerometer BMA220 in the front trouser pocket, each subject performed 8 types of activities of daily living such as Walking, Standing, Sitting and 9 types of falls such as Falling leftward, Falling rightward, Falling back and Syncope. All samples were collected at a frequency of 50 Hz.

5) OPPORTUNITY[49]: The dataset was collected from various hybrid sensor modalities such as accelerometer, gyroscope, magnetometer, and video camera. In a breakfast scenario, 12 volunteers are instructed to perform a specific set of daily morning activities such as Preparing and Drinking coffee, Preparing and Eating sandwich, and Cleaning table. In this paper, we utilize the subset from the OPPORTUNITY challenge consisting of unsegmented sensor recordings from 4 subjects. Data is collected at a sampling rate of 30Hz by the body-worn sensors placed on 12 different locations of human body.

B. Training details

We perform experiments on the five benchmark HAR datasets: UCI-HAR, WISDM, PAMAP2, UniMib-SHAR, and OPPORTUNITY. Data preprocessing is a crucial step in this activity recognition process. Sensor signals are often involved in various human activities in different contexts, which have been recorded via hybrid sensor modalities. The heterogeneous sensor values have to be normalized into zero mean and unit variance via subtracting the mean and dividing by the standard deviation. Traditional machine learning algorithms could not directly handle raw sensor input, which need to be first segmented via a fixed-length sliding window. To be specific, fixing an overlap rate, one can slide window over continuous sensor reading to produce continuous samples, where each window may be assigned a specific activity label. As a result, data are divided into windows of a fixed size and with no inter-window gaps, and an overlap between adjoining windows is tolerated to preserve the continuity of sensor signals. Although sliding window has been normally used to perform segmentation, there is still no clear consensus on how to select an optimal window size. Actually, the window size has an important effect on activity recognition performance[50]. According to our intuition, reducing the window length will be more beneficial for a faster activity recognition, as well as reduced computational cost and energy consumption. Instead, increasing window length are usually used for the recognition of complex activities that last a longer time. Actually, most designs normally rely on figures used in previous works, but with no strict researches that support them. For fair comparisons, we still select the same values used in previous HAR literatures. During data preprocessing stage, several important properties such as window size, overlap rate and sampling rate are summarized in Table I. All datasets are divided into three parts consisting of a training set (70%), a validation set (10%) and a test set (20%).

All detailed training parameters are provided for reproducibility. On each dataset, the 3-layer tunable width network equipped with triangular convolutional layers is compared with normal baseline CNN. The detailed descriptions of network architectures are illustrated in Table II. Each convolutional (Conv) layer is followed by a batch-normalization (BN) layer and activation function (ReLU). Batch normalization plays a role in standardizing the inputs to a layer for each mini-batch, which has an effect of stabilizing the learning process and dramatically reducing the number of training epochs required to train deep networks. In particular, three lower-triangular convolutional layers are stacked in order to remove the impact of activation statistics caused by varying widths. The max-pooling operation pools a feature map by taking its maximum values. Two max-pooling operations are inserted after the second and third convolutional layers. In the case of activity recognition task, the final output may be further fed into a Softmax layer to produce a class
probability distribution. We introduce the detailed parameter settings of low-triangular convolution, such as kernel size, step length and padding size in Table III. The source code will be available at the website https://github.com/Chauncey-Wang/Tunable-Speed-Accuracy-Trade-off-for-HAR. During each training iteration, all networks are trained at eight random sampling widths. That is to say, we train all eight widths as sub-networks simultaneously by accumulated their losses. We use the random sampling strategy as indicated above in Section III. All networks are trained for 200 epochs by using an Adam optimizer with batch size of 512. The initial learning rate is set to 5e-4, which is decayed by a factor of 0.1 every 40 epochs. All experiments are implemented by deep learning library PyTorch on a workstation equipped with Intel I7-6850K CPU, NVIDIA GeForce RTX3090 GPU and 64G RAM. Main experiments results are presented in Table IV at eight width factors of 0.125, 0.25, 0.375, 0.5, 0.625, 0.75, 0.875, 1.0. It can be seen that our tunable width networks perform as well or better than its normal CNN counterparts. In terms of accuracy, our models outperform their normal baselines by 0.35%, 0.72%, 0.87%, 0.60% and 0.08% respectively at the same width of 1. In an extreme case where the network width is reduced to 0.125x, there are only 0.96%, 0.96%, 1.29%, 0.80% and 0.08% performance degradation when compared with 1.0x(Fig.3). As an acknowledged limitation caused by the trade-off between accuracy and speed, the accuracy drops are an expected behavior, which is totally acceptable for multi-width HAR applications. From an aspect of computational overhead, it is worthwhile to mention that the triangular convolutional layer itself can roughly halve the number of total parameters, where accuracy only slightly decays as network width decreases. In addition, we also measure the number of multiply-add operations (MAC) and inference time(Table V). Due to the lower-triangular design constrain, the computational complexity is significantly reduced. As illustrated in Fig.4 and Fig.5, if one decreases the width factor, the inference time can rapidly decay while the precisions of prediction still can maintain parity.

C. Albation experiment

In order to explore why the lower-triangular convolution can perform better in multi-width HAR scenario, we implement two network architectures: a normal CNN, a tunable width CNN constructed by lower-triangular convolutional layers. For simplicity, we train both models on UCI-HAR dataset at four different widths of 0.25, 0.5, 0.75, 1.0. During training, the means of 1st-layer and variances of 3rd-layer are accumulated from batch normalization layer. At different widths, we compare the means and variances of selected channel. Fig.6 and Fig.7 shows that there is a noticeable deviation of activation statistics within normal CNN if width is varied, which is consistent with our expectation. In other words, different widths produce different activation statistics, which leads to worse performance. Replacing normal convolution with lower-triangular convolution, we could clearly see that lower-triangular weight constrain significantly converges better, which can help to stable activation statistics. It will be more beneficial for providing higher and more consistent validation accuracy when one switches network between different widths.

We continue to investigate how the number of randomly sampled widths (i.e., N) affects classification performance, because too large N will lead to unnecessary training burden. During each iteration, we train our models on PAMAP2 and WISDM datasets when N is set to 1, 2, 4, 8 and 16 respectively. Fig.8 shows that the classification performance will decay rapidly as network width decreases if we perform only one or two sampling. It can be seen that the models
Fig. 6. Mean of standard CNN and triangular CNN trained with N= 4, 8 and 16 significantly outperform those with N = 1 and 2. The classification accuracy starts to saturate or even drop if N become relatively large (e.g., N = 16). N = 8 is the default through all our experiments.

As indicated in above Eq.2, there is a lower bound $k_0$, which plays an important role in controlling width. In order to examine how the lower bound influences final classification performance, we perform the evaluation on UCI-HAR dataset, under four different width lower bounds as 0.0625, 0.125, 0.25, and 0.375. As illustrated in Fig.9 and Fig.10, it can be observed that $k_0=0.125$ has obviously better performance. Compared with $k_0=0.0625$, a smaller sampling interval is usually enough to produce satisfactory accuracy. The results indicate that the classification accuracy depends on the width lower bound, it is totally feasible to sample width between the interval [0.125, 1].

We further investigate the effectiveness of random width sampling strategy. Four cases are evaluated: N random widths without a minimum width and a maximum width; N-1 random widths without a minimum width; N-1 random widths without a maximum width; N-2 random widths with a minimum width and a maximum width. As we can see, the total number of sampling widths is set to N. In the first case, the total N random widths need to be sampled because both a minimum width and a maximum width are not fixed. In the second or third case, only N-1 random widths need to be sampled because either a minimum width or a maximum width is already fixed. In the fourth case, only N-2 random widths need to be sampled because two widths, i.e., a minimum width and a maximum width are already fixed. The evaluations are performed on UCI-HAR dataset. Fig.11 and Fig.12 emonstrate that the models trained with a minimum width and a maximum width perform better than those without a minimum width and a maximum width.

In addition, the model trained with lower bound has higher accuracy than that with upper bound, which indicates the importance of lower bound $k_0$. Thus, we train all models by fixing lower bound and upper bound.

To verify the effectiveness of the proposed model on a resource-constrained edge device, we deploy the flexible HAR system into a Raspberry Pi 3B+ equipped with an official supported Raspberry Pi operating system. It has a good compatibility with the deep learning library PyTorch 1.7 used in our experiments. The model is trained on WISDM dataset. We run it on the embedded platform to read one sensor sample and perform an online prediction. A Python program...
is developed for the HAR application. Fig. 13 illustrates the graphical user interface (GUI) of the application, which is able to tune network width, show prediction probability of each activity and calculate inference time. We compare the inference time at different widths e.g., 0.125, 0.5, and 1.0, and results are shown in Table VI. As network width increases, it takes around 52.901~68.591ms, 101.434~125.847ms and 147.261~167.773ms respectively to predict one ten-second window.

We further add the results of real experiments based on

![Fig. 8. The speed-accuracy trade-off curves at different sampling number](image1)

![Fig. 9. The speed-accuracy trade-off curves at different width lower bounds](image2)

![Fig. 10. Performance of different width lower bounds](image3)

![Fig. 11. The speed-accuracy trade-off curves at different sampling rules](image4)

![Fig. 12. Performance of different sampling rules](image5)

![Fig. 13. GUI of the HAR application on Raspberry Pi](image6)

![Fig. 14. Experimental demonstration of application on Raspberry Pi 3B+](image7)
the proposed HAR system. For practical implementation, we choose a 3-axis accelerometer (adx1345) as IMU and communicate it with Raspberry Pi 3B+ via Inter-Integrated Circuit (I2C). We configure Wi-Fi on the Raspberry Pi so as to access it remotely via a laptop computer. As shown in Fig. 14, following the experiment settings in WISDM dataset, the IMU node is attached to the subjects front leg pocket. The main functions are composed of two independent threads process: ProcessSignals and OnlinePrediction. The former is charge of communicating with Raspberry Pi and periodically reads sensor signals, and then data normalized is done by using the mean and standard deviation of training data. The latter is charge of predicting activities. For the

<table>
<thead>
<tr>
<th>Width Multiplier</th>
<th>Time/ms</th>
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<tbody>
<tr>
<td>0.125</td>
<td>52.901–68.591</td>
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<tr>
<td>0.50</td>
<td>101.434–125.847</td>
</tr>
<tr>
<td>1.0</td>
<td>147.261–167.773</td>
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Fig. 15. Inference time

WISEM case, a ten-second window with an 95% overlap rate is slide over real sensor readings recorded from the IMU node to generate one sample. Thus, the step length is equal to 500ms, and the recognition system will wait for 500ms to read and predict next sample. That is to say, OnlinePrediction is triggered by scheduled interruptions every 500ms that correspond to 5% of window length. We set three widths to implement activity inference for 500 runs. The inference times with different widths are shown in Fig. 15. Overall, the experimental results verify that the proposed method can obtain an efficient speedup for activity inference at much smaller memory footprint.

The measured values are collected from two subjects, and the collection process is illustrated in Fig. 14. Each subject performs six types of activities: Walking, Jogging, Upstairs, Downstairs, Sitting, and Standing. The embedded measuring system still maintains a sampling rate of 20Hz, where a fixed-length sliding window of 10 seconds and an 95% overlap rate are used to segment raw sensor readings (i.e., 200 raw accelerometer readings per sample). The measured sensor values need to be standardized into zero mean and unit variance. Overall, the test set is composed of 2,282 samples, whose statistics is shown in Table VII. To verify the effectiveness of our model, we summarize our results of the embedded measuring system in Fig. 16. In order to show the predictive accuracy associated with each of the activities done by the system, we compute the confusion matrices that contains information about actual and predicted activity classifications. For example, in the case of the activity Jogging, the CNN with width factor 1 makes 5 errors, while the CNNs with width factor 0.5 and 0.125 make 6 and 9 errors respectively. Similarly, for the activity Upstairs, the CNN with width factor 1 makes 45 errors, while the CNNs with width factor 0.5 and 0.125 misclassifies 58 and 77 samples respectively. The results indicate that the classification performance only decays slightly as the width factor decreases, which is in line with our prior results.

V. CONCLUSION

Decent recent years, deep learning has achieved state-of-the-art performance in sensor based HAR area. However, real HAR applications are often deployed across different wearable devices or hardware versions. Thus, an important issue is how to maintain model flexibility for adapting quickly to new computing platform, which has rarely been investigated so far. In this paper, we propose an tunable width convolutional neural network to perform activity recognition on resource-constrained wearable devices. Specially, the network is stacked by lower-triangular convolutional layers rather than normal convolution to avoid the influence of varying batch statistics caused by the switch between multiple widths. The lower-triangular constrains is very suitable for tunable width networks. To acquire smooth control over width for the trade-off between speed and accuracy, we perform random sampling rather than fixed sampling over width, where the network at different widths can be trained simultaneously as sub-networks by accumulating their losses. Evaluation results validate the practicability and effectiveness of the proposed HAR model, compared with normal CNN.

At present, there are at least 24,000 Android devices, which have drastically different computing resources. Even for the same device, the inference speed also always varies due to excessive consumption caused by background apps that decreases the available computational budget. In addition, it will take extra time and data for downloading and offloading models when switching to a larger or smaller model. However, at runtime prior networks need to be re-configured for adapting across different devices for a given response time. This paper attempts to handle this issue: For a given computational
budget, how to adaptively tradeoff accuracy and speed for activity inference at runtime? We propose a tunable-width neural network as a potential solution, which can be executed at different widths. For brevity, the network may be easily varied for a switch by tuning its width, i.e., the number of channels alone. That is to say, we only need to change network width without the need of redownloading or offloading new models. Comparing to prior static networks, our method has several advantages: (1) For different computational budget, a single HAR model is trained. (2) A near-optimal trade-off between accuracy and speed can be flexibly deployed on a target device by adjusting network width accordingly. (3) The solution is generally applicable to popular mainstream building blocks of neural networks such as convolutions or fully-connected layers, etc. Overall, it is easier to be deployed on wearable or mobile devices with existing deep learning libraries, which could be a better strategy to perform activity inference without extra computational and memory cost. Our research provides a new research direction for building flexible models for activity inference on resource-constrained wearable devices.

REFERENCES

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